

The Automobile and the Environment

The Automobile and the Environment:
International Congress of Automotive
and Transport Engineering CONAT 2010

Edited by

Anghel Chiru

**CAMBRIDGE
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P U B L I S H I N G

The Automobile and the Environment:
International Congress of Automotive and Transport Engineering CONAT 2010,
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FOREWORD

The automobile - miracle of this century, and the industries which contribute to its production, incorporate results of the high competitions in engineering creation and innovation, obtained under conditions of severe selections made in conjunction with the values of human society, culture and life style of local communities, sustainable development and environmental protection.

The development of strategic concepts for future automobiles involves a great scientific and technical cooperation between research institutes, manufacturing companies, major universities and local governments. This involves the development of highly complex researches, covering:

- advanced design, modeling and simulation procedures, controlled by powerful information systems;
- new modern materials, innovative manufacturing and assembling technologies that allow to identify the technical solutions for high productivity;
- alternative fuels, sustainable development, recycling and environment protection;
- advanced testing, analysis and validation technologies;
- vehicles with alternative propulsion systems, attractive and environmental responsible; management of the propulsion sources, braking energy recovery, driving facilitate and comfort improvement;
- the mechatronic architectures that facilitate the development of engine systems and automotive engineering;
- performant road traffic and safety with benefits in accident reconstruction; objective perception of the relationship between people-environment-vehicle-road safety assessment;
- lifecycle analysis as a holistic approach; vehicle reliability and risk assessment.

Wishing to respond to major challenges set out by the themes presented, in terms of restructuring the research and innovation policies and programs, of global production capacities resizing, defining new strategic alliances, development of emerging markets, increasing the competitiveness and requirements imposed in projects selection, we selected for this volume 43 scientific papers, from the 260 papers produced and presented by specialists from academic institutions, companies and research institutes from 22

countries, which were held in the sessions of the International Congress for Automotive and Transport Engineering CONAT 2010. The selected papers were focused and structured on four key themes which covered the topics:

- Automotive Powertrains
- Alternative Fuels
- Vehicle Dynamics, Vehicle Systems Design
- Transport, Traffic and Safety.

The scientific and technical information presented are intended for those who design, research, optimize and manufacture automobiles, equipment and components, technologies, innovative materials and processes, road traffic networks and systems, security systems and smart cars. They are also useful for many specialists who create installations, processes and equipment that enable the development of new propulsion sources for future vehicles, alternative fuels recipes, techniques for recycling and environmental protection.

Regarding the International Congress CONAT 2010 (XI-th edition, 27-29 October 2010), organized by SIAR – the Society of Automotive Engineers of Romania, Transilvania University of Braşov and SAE International, under the patronage of FISITA (International Federation of Automotive Engineering Societies) and EAEC (European Automobile Engineers Cooperation), it must be highlighted that this event was dedicated to celebration of 61 years of the Automotive School at Transilvania University and 20 years after founding SIAR.

This book was possible to be realized in this form thanks to the help of Mr. Dinu Covaciu, Ph.D., researcher at Transilvania University of Braşov. In all the activities he has undertaken, from manuscript to final form, I noticed the scientific rigor, determination and organization effectiveness. I wish to thank also for their help to my colleagues: Prof.Eng. Gheorghe Alexandru Radu, Ph.D., eng. Ruxandra Cristina Dica, Ph.D. Candidate, and also to all the collaborators from the Automotive Engineering Department of the Transilvania University.

To Mr. Brigadier ret. Prof. Günter Hohl, EAEC President, and to Mr. Dipl.Ing. Eduard Golovatai-Schmidt, Manager Advance Development Engine Systems at Schaeffler Technologies GmbH & Co.KG, I wish to present my deep gratitude for their interest and involvement in the organization of the CONAT 2010 Congress and the realization of this book.

Braşov, 04.04.2011

Anghel CHIRU

Prof.Eng., Ph.D.

Chairman of the Congress CONAT 2010

PART I:
AUTOMOTIVE POWERTRAINS

CHAPTER ONE

THERMODYNAMIC ASPECTS OF POWER PRODUCTION IN ENERGY SYSTEMS

STANISLAW SIENIUTYCZ

Introduction

Applications of thermodynamics of finite rates lead to solutions which describe various forms of bounds on power and energy production (or consumption), including, in dynamical cases, finite-rate generalizations of the standard availabilities. In this research, we treat power limits in static and dynamical energy systems driven by nonlinear fluids that are restricted in their amount or magnitude of flow and, as such, play the role of resources. A power limit is an upper (or lower) bound on power produced (or consumed) in the system. A resource is a valuable substance or energy used in a process; its value can be quantified by specifying its exergy, a maximum amount of work that can be obtained when the resource relaxes to the equilibrium. Reversible relaxation of the resource is associated with the classical exergy. When dissipative phenomena prevail, generalized exergies are essential. In fact, generalized exergies quantify deviations of the system's efficiency from the Carnot efficiency. An exergy is obtained as the principal component of the solution to the variational problem of extremum work under suitable boundary conditions. Other components of the solution are optimal trajectory and optimal control. In purely thermal systems (those without chemical changes), the trajectory is characterized by temperature of the resource fluid, $T(t)$, whereas the control is Carnot temperature $T'(t)$ defined in our previous work [1, 2]. For chemical systems, chemical potential(s) $\mu'(t)$, also play a role. Whenever $T'(t)$ and $\mu'(t)$ differ from $T(t)$ and $\mu(t)$ the resource relaxes with a finite rate, and with an efficiency vector different from the perfect efficiency. Only when $T' = T$ and $\mu' = \mu$ is the efficiency perfect, but this corresponds with an infinitely slow relaxation rate of the resource to the thermodynamic equilibrium with the environmental fluid.

The structure of this paper is as follows: Section II discusses various aspects of power optimization. Properties of steady systems are outlined in Sec. III, whereas those of dynamical ones are found in Sec. IV. Section V develops quantitative analyses of resource downgrading (in the first reservoir) and outlines properties of generalized potentials for finite rates. Sections VI-VIII discuss various Hamilton-Jacobi-Bellman equations (HJB equations) for optimal work functions as solutions of power yield problems. Extensions for simple chemical systems are outlined in Sec. IX, while fuel cells are considered in Sec. X.

The size limitation of our paper does not allow for inclusion of all derivations to make the paper self-contained, thus the reader may need to turn to some previous works, [1] - [5]. In view of difficulties in getting analytical solutions in complex systems, difference equations and numerical approaches are treated in ref. [3], which also discusses convergence of numerical algorithms to solutions of HJB equations and role of Lagrange multipliers in the dimensionality reduction.

Finite Resources and Power Optimization

Limited amount or flow of a resource working in an engine causes a decrease of the resource potential in time (chronological or spatial). This is why studies of resource downgrading apply the dynamical optimization methods. From the optimization viewpoint, a dynamical process is every one with a sequence of states, developing either in chronological time or in (spatial) holdup time. The first group refers to unsteady processes in non-stationary systems; the second group may involve steady state systems.

In a process of energy production, two resting reservoirs do interact through an energy generator (engine). In this process, power flow is steady only when the two reservoirs are infinite. When one, say, upper, reservoir is finite, its thermal potential must decrease in time, which is a consequence of the energy balance. Any finite reservoir is thus a resource reservoir. It is the resource property that leads to the dynamical behaviour of the fluid and its relaxation to the equilibrium with an infinite lower reservoir (usually the environment).

Alternatively, fluid at a steady flow can replace the resting upper reservoir. The resource downgrading is then a steady-state process in which the resource fluid flows through a pipeline or stages of a cascade and the fluid's state changes along a steady trajectory. As in the previous case, the trajectory is a curve describing the fluid's relaxation towards the equilibrium between the fluid and the lower reservoir (the environment). This is sometimes called "active relaxation" as it is associated with

simultaneous work production. It should be contrasted with “dissipative relaxation”, a well-known, natural process between a body or a fluid and the environment without any power production.

Relaxation (either active or dissipative) leads to a decrease of the resource potential (i.e. temperature) in time. An inverse of the relaxation process is the one in which a body or a fluid abandons the equilibrium. This cannot be spontaneous; rather the inverse process needs a supply of external power. This is the process referred to as thermal upgrading of the resource, which can be accomplished with a heat pump.

Steady Systems

A great deal of the research on power limits published to date deals with stationary systems, in which case both reservoirs are infinite. For this case, refer to the steady-state analyses of the Chambadal-Novikov-Curzon-Ahlborn engine (CNCA engine [6]), in which energy exchange is described by the Newtonian law of cooling, or the Stefan-Boltzmann engine, a system with radiation fluids and energy exchange governed by the Stefan-Boltzmann law [7]. Due to their stationarity (caused by the infiniteness of both reservoirs), controls maximizing power are lumped to a fixed point in the state space. In fact, for the CNCA engine, the maximum power point may be related to the optimum value of a free (unconstrained) control variable, which can be efficiency η or Carnot temperature T' . In terms of the reservoirs' temperatures T_1 and T_2 and the internal irreversibility factor Φ one finds $T'_{opt} = (T_1\Phi T_2)^{1/2}$ [4]. For the Stefan-Boltzmann engine, the exact expression for the optimal point cannot be determined analytically, yet, this temperature can be found graphically from the chart $P=f(T')$.

Moreover, the method of Lagrange multipliers can successfully be applied [8]. As their elimination from a set of resulting equations is quite easy, the problem is broken down to the numerical solving of a nonlinear equation for the optimal control T' . Finally, the so-called pseudo-Newtonian model [4, 5], which uses state or temperature dependent heat exchange coefficient, $\alpha(T^3)$, omits, to a considerable extent, analytical difficulties associated with the Stefan-Boltzmann equation. Applying this model in the so-called symmetric case, where both reservoirs are filled up with radiation, one shows that the optimal (power maximizing) Carnot temperature of the steady radiation engine is that of the CNCA engine, i.e. [4]. This equation is, in fact, a good approximation under the assumption of transfer coefficients dependent solely on bulk temperatures of reservoirs.

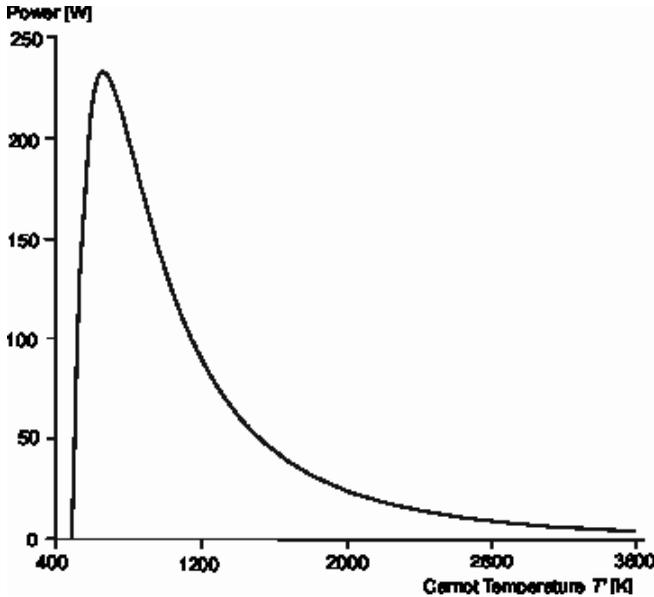


Fig. 1 Maximum power relaxation curve for black radiation without constraint on the temperature [8].

Dynamical Systems

The evaluation of dynamical energy yield requires knowledge of an extremal curve rather than an extremum point. This is associated with application of variational methods (to handle functional extrema) in place of static optimization methods (to handle extrema of functions). For example, the use of the pseudo-Newtonian model to quantify the dynamical energy yield from radiation, gives rise to an extremal curve describing the radiation relaxation to the equilibrium. This curve is non-exponential, the consequence of the nonlinear properties of the relaxation dynamics. There are also other non-exponential curves describing the radiation relaxation, e.g. those following from exact models using the Stefan-Boltzmann equation (symmetric and hybrid, [4,5]).

Analytical difficulties associated with dynamical optimization of nonlinear systems are severe; this is why diverse models of power yield, and diverse numerical approaches, are applied. An optimal (e.g. power-maximizing) relaxation curve $T(t)$ is associated with the optimal control curve $T'(t)$; they are both components of the dynamic optimization solution to a continuous problem. In the corresponding discrete problem, formulated

for numerical purposes, one searches for optimal temperature sequences $\{T^n\}$ and $\{T'^n\}$. Various discrete optimization methods involve: direct search, dynamic programming, discrete maximum principle, and combinations of these methods.

Minimum power supplied to the system is described in a suitable way by function sequences $R^n(T^n, t^n)$, whereas maximum power produced – by functions $V^n(T^n, t^n)$. Profit-type performance function V and cost-type performance function R simply differ by sign, i.e. $V^n(T^n, t^n) = -R^n(T^n, t^n)$. The beginner may find the change from symbol V to symbol R and back as unnecessary and confusing. Yet, each function is positive in its own, natural regime of working (V - in the engine range, and R - in the heat pump range).

Importantly, energy limits of dynamical processes are inherently connected with the exergy functions, the classical exergy, and its rate-dependent extensions. To obtain classical exergy from power functions it suffices to assume that the thermal efficiency of the system is identical with the Carnot efficiency. On the other hand, non-Carnot efficiencies lead to generalized exergies. The latter depend not only on classical thermodynamic variables but also on their rates. These generalized exergies refer to state changes in a finite time, and can be contrasted with the classical exergies that refer to reversible quasistatic processes evolving in time infinitely slowly. The benefit obtained from generalized exergies is that they define stronger energy limits than those predicted by classical exergies.

A systematic approach to exergies (classical or generalized) based on work functionals leads to several original results in thermodynamics of energy systems, in particular it allows explanation of unknown properties of exergy of black-body radiation or solar radiation, and to show that the efficiency of the solar energy flux transformation is equal to the Carnot efficiency. To date this has not been a commonly accepted result, as a number of recent investigations show.

Towards a Finite-Rate Exergy

Two different works, the first associated with resource downgrading during its relaxation to the equilibrium, and the second with the reverse process of resource upgrading, are essential (Fig.2). During the approach to equilibrium, the engine mode takes place in which work is released; during the departure, the heat-pump mode occurs in which work is supplied. Work W delivered in the engine mode is positive by assumption (“engine convention”). A sequence of irreversible engines (CNCA or

Stefan-Boltzmann) serves to determine a rate-dependent exergy extending the classical exergy for irreversible, finite rate processes. Before maximization of a work integral, process efficiency η has to be expressed as a function of state T and a control, i.e. energy flux q or rate $dT/d\tau$, to assure the functional property (path dependence) of the work integral. The integration must be preceded by maximization of power or work at flow (the ratio of power and flux of driving substance) w to assure an optimal path.

The optimal work is sought in the form of a potential function that depends on the end states and duration.

For appropriate boundary conditions, the principal function of the variational problem of extremum work coincides with the notion of an exergy, the function that characterizes quality of resources. The idea of an infinite number of infinitesimal CNCA steps, necessary for exergy calculations, is illustrated in Fig.2. Each step is a work-producing (consuming) stage with the energy exchange between two fluids and the thermal machine through finite “conductances”.

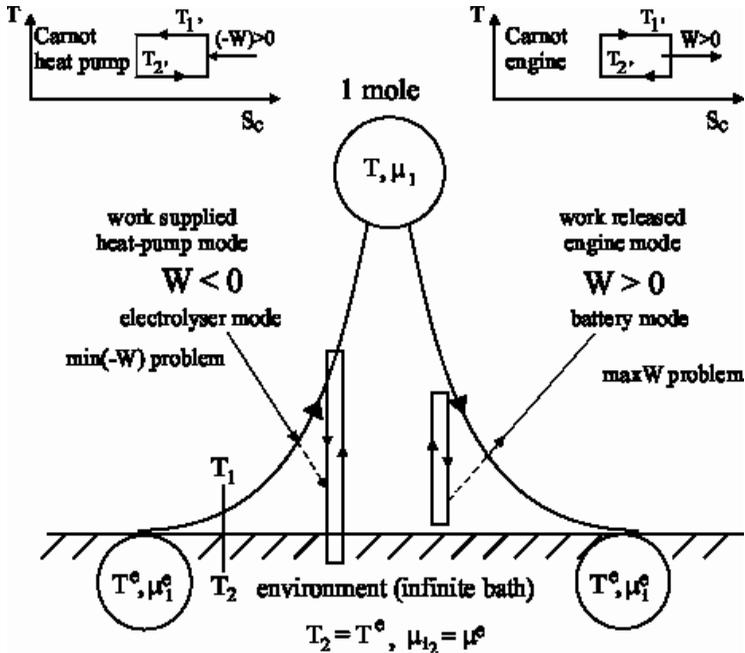


Fig. 2 Two works: Limiting work produced and limiting work consumed are different in an irreversible process.

For the radiation engine, it follows from the Stefan-Boltzmann law that the effective transfer coefficient α_1 of the radiation fluid is necessarily temperature dependent; $\alpha_1 = \propto T_1^3$. The second or low- T fluid represents the usual environment, as defined in the exergy theory. This fluid possesses its own boundary layer as a dissipative component, and the corresponding exchange coefficient is α_2 . In the physical space, the flow direction of the resource fluid is along the horizontal coordinate x . The optimizer's task is to find an optimal temperature of the resource fluid along the path that extremizes the work consumed or delivered.

Total power obtained from an infinite number of infinitesimal engines is determined as the Lagrange functional of the following structure

$$\dot{W}[\mathbf{T}^i, \mathbf{T}^f] = \int_{t^i}^{t^f} f_0(T, T') dt = - \int_{t^i}^{t^f} \dot{G}c(T)\eta(T, T')\dot{T} dt \quad (1)$$

where f_0 is power generation intensity, \dot{G} - resource flux, $c(T)$ - specific heat, $\eta(T, T')$ - efficiency in terms of state T and control T' , also \mathbf{T} - enlarged state vector comprising state and time, t - time variable (residence time or holdup time) for the resource contacting with heat transfer surface. Sometimes one uses a non-dimensional time τ , identical with the so-called number of the heat transfer units. Note that, for constant mass flow of a resource, one can extremize power per unit mass flux, i.e. the quantity of work dimension called "work at flow". In this case Eq. (1) describes a problem of extremum work. Integrand f_0 is common for both modes, yet the numerical results it generates differ by sign (positive for engine mode; "engine convention"). When the resource flux is constant, a work functional describing the thermal exergy flux per unit flux of resource can be obtained from Eq. (1)

$$w_{\max}^{\frac{dT}{dt}} = - \int_{T=T^i}^{T^e=T^f} c(T) \left(1 - \frac{T^e}{T'(T, dT/dT)} \right) dT \quad (2)$$

Note that the independent variable in this equation is T , i.e. it is different from that in Eq. (1).

The function f_0 in Eq. (1) contains thermal efficiency function, η , described by a practical counterpart of the Carnot formula. When $T > T^e$, efficiency η decreases in the engine mode above η_C and increases in the heat-pump mode below η_C . At the limit of vanishing rates, $dT/dt = 0$ and

$T' \rightarrow T$. Then the work of each mode simplifies to the common integral of the classical exergy. For the classical thermal exergy

$$w_{\max}^{\frac{dT}{dt} \rightarrow 0} = - \int_{T=T^i}^{T^e=T^f} c(T) \left(1 - \frac{T^e}{T} \right) dT = h - h^e - T^e (s - s^e) \quad (3)$$

Nonlinearities can have both thermodynamic and kinetic origins; the former refer, for example, to state dependent heat capacity, $c(T)$, the latter to nonlinear energy exchange. Problems with linear kinetics (Newtonian heat transfer) are an important subclass. In problems with linear kinetics, a fluid's specific work at flow, w , is described by an equation

$$w[\mathbf{T}^i, \mathbf{T}^f] = \dot{W} / \dot{G} = - \int_{T^i}^{T^f} c(T) \left(1 - \frac{T^e}{T} \right) dT = -T^e \int_{T^i}^{T^f} c(T) \frac{(T' - T)^2}{T T'} d\tau \quad (4)$$

where

$$\tau \equiv \frac{x}{H_{TU}} = \frac{\alpha' a_v F}{\dot{G} c} x = \frac{\alpha' a_v F v}{\dot{G} c} t = \frac{t}{\chi} \quad (5)$$

is non-dimensional time of the process. Equation (5) assumes that a resource fluid flows with velocity v through cross-section F and contacts with the heat transfer exchange surface per unit volume a_v [1]. Quantity τ is identical with the so-called number of the heat transfer units.

Solutions to work extremum problems can be obtained by:

a) variational methods, i.e. via Euler-Lagrange equation of variational calculus

$$\frac{\partial L}{\partial T} - \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{T}} \right) = 0 \quad (6)$$

In the example considered above, i.e. for a thermal system with linear kinetics

$$T \frac{d^2 T}{d\tau^2} - \left(\frac{dT}{d\tau} \right)^2 = 0 \quad (7)$$

which corresponds with the optimal trajectory

$$T(\tau, \tau^f, T^i, T^f) = T^i (T^f / T^i)^{\tau / \tau^f} \quad (8)$$

($\dot{\tau} = 0$ is assumed in Eq. (8).) However, the solution of Euler-Lagrange equation does not contain any information about the optimal work function. This is assured by solving the Hamilton-Jacobi-Bellman equation (HJB equation, [9]).

b) dynamic programming via the HJB equation for the ‘principal function’ (V or R), also called extremum work function. For the linear kinetics considered

c)

$$\frac{\partial V}{\partial \tau} - \max_{T'} \left\{ \left(-\frac{\partial V}{\partial T} - c \left(1 - \frac{T^e}{T'} \right) \right) (T' - T) \right\} = 0 \quad (9)$$

Observe that all rates (f_0 and f) and derivatives of V are evaluated at the final state (the so-called ‘forward equation’). The extremal work function V is a function of the final state and total duration. After evaluation of optimal control and its substitution to Eq. (9), one obtains a nonlinear equation

$$\frac{\partial V}{\partial \tau} - c \left\{ \sqrt{T^e} - \sqrt{T(1 + c^{-1} \partial V / \partial T)} \right\}^2 = 0 \quad (10)$$

which is the Hamilton-Jacobi equation of the problem. Its solution can be found by the integration of work intensity along an optimal path, between limits T and T^f . A reversible (path independent) part of V is the classical exergy $A(T, T^e, 0)$.

Details of models of multistage power production in sequences of infinitesimal engines are known from previous publications [1]-[5]. These models provide power generation functions f_0 or thermal Lagrangians $l_0 = -f_0$ and dynamical constraints. Numerical methods apply suitable discrete models, for given rates f_0 and f . An important issue is convergence of these discrete models to continuous ones [3].

HJB Equations for Nonlinear Power Systems

We shall display here some Hamilton-Jacobi-Bellman equations for power systems described by nonlinear kinetics. A suitable example is a radiation engine whose power integral is approximated by a pseudo-Newtonian model of radiative energy exchange associated with optimal function

$$V(T^i, t^i, T^f, t^f) \equiv \max_{T'(t)} \left(- \int_{t^i}^{t^f} \dot{G}_m c_m (1 - \Phi' \frac{T^e}{T'}) \nu(T', T) dt \right) \quad (11)$$

where $\nu = \alpha(T^3)(T' - T)$. An alternative form uses Carnot temperature T' explicit in ν [5]. Optimal power (11) can be referred to the integral

$$\begin{aligned} \dot{W} = & - \int_T^{T_0} \dot{G}_m \left(c_{hm}(T) - c_{vm}(T) \frac{T^e}{T} \right) \nu dt \\ & - \int_T^{T_0} T^e \dot{G}_m \left(c_{vm}(T) \left(\frac{\chi \nu^2}{T(T + \chi \nu)} + (1 - \Phi) \frac{\nu}{T + \chi \nu} \right) \right) dt \end{aligned} \quad (12)$$

This process is described by a pseudolinear kinetics $dT/dt = f(T, T')$ consistent with $\nu = \alpha(T^3)(T' - T)$ and a general form of HJB equation for work function V is

$$- \frac{\partial V}{\partial t} + \max_{T'(t)} \left(f_0(T, T') - \frac{\partial V}{\partial T} f(T, T') \right) = 0 \quad (13)$$

where f_0 is defined as the integrand of Eq. (11) or (12).

A more exact model of radiation conversion relaxes the assumption of the pseudo-Newtonian transfer and applies the Stefan-Boltzmann law. For a *symmetric* model of radiation conversion (both reservoirs composed of radiation)

$$\dot{W} = \int_{t^i}^{t^f} \dot{G}_c \left(1 - \frac{\Phi T^e}{T'} \right) \beta \frac{T^a - T'^a}{(\Phi'(T'/T^e)^{a-1} + 1) T'^{a-1}} dt \quad (14)$$

The coefficient $\beta = \sigma \alpha_v c_h^{-1} (p_m^0)^{-1}$ is related to molar constant of photons density p_m^0 and Stefan-Boltzmann constant σ . In the physical space, power exponent $a=4$ for radiation and $a=1$ for a linear resource. With state equation

$$\frac{dT}{dt} = -\beta \frac{T^a - T'^a}{(\Phi'(T'/T^e)^{a-1} + 1) T'^{a-1}} \quad (15)$$

[5], applied in general Eq. (19), we obtain a *HJB* equation

$$-\frac{\partial V}{\partial t} + \max_{T'(t)} \left\{ \left(\dot{G}_c (1 - \Phi \frac{T^e}{T'}) + \partial V / \partial T \right) \times \beta \frac{T^a - T'^a}{(\Phi'(T'/T_2)^{a-1} + 1) T^{a-1}} \right\} = 0 \quad (16)$$

Dynamics (15) is the characteristic equation for Eq. (16).

For a *hybrid model* of radiation conversion (upper reservoir composed of the radiation and lower reservoir of a Newtonian fluid, [5]) the power is

$$\dot{W} = - \int_{\tau'}^{\tau^f} G_c(T) \left(1 - \frac{\Phi T^e}{(T^a + \beta^{-1} T^{a-1} u)^{1/a} + \Phi \beta^{-1} T^{a-1} u g_1 / g_2} \right) u dt \quad (17)$$

and the corresponding Hamilton-Jacobi-Bellman equation is

$$-\frac{\partial V}{\partial t^f} + \max_{T'(t)} \left\{ - \left(\dot{G}_c(T) \left(1 - \frac{\Phi T^e}{(T^a + \beta^{-1} T^{a-1} u)^{1/a} + \Phi \beta^{-1} T^{a-1} u g_1 / g_2} \right) + \frac{\partial V}{\partial T^f} \right) u \right\} = 0 \quad (18)$$

Analytical Aspects of Linear and Pseudo-Newtonian Kinetics

In all HJB equations extremized expressions are hamiltonians. Applying the feedback control optimal driving temperature T' , or other control, is implemented as the quantity maximizing the hamiltonian with respect to T' at each point of the path. The maximization of H leads to two equations. The first expresses optimal control T' in terms of T and $z = -\partial V / \partial T$; for Eq. (9) we find

$$\frac{\partial V}{\partial T} - \frac{\partial f_0(T, T')}{\partial T'} = \frac{\partial V}{\partial T} + c \left(1 - \frac{T^e T}{T'^2} \right) = 0 \quad (19)$$

whereas the second is the original equation (9) without the maximizing operation

$$\frac{\partial V}{\partial \tau} + \frac{\partial V}{\partial T} (T' - T) + c \left(1 - \frac{T_2}{T'} \right) (T' - T) = 0 \quad (20)$$

To obtain optimal control function $T(z, T)$ one should solve the second equality in equation (19) in terms of T . The result is Carnot control T' in terms of T and $z = -\partial V/\partial T$,

$$T' = \left(\frac{T^e T}{1 + c^{-1} \partial V / \partial T} \right)^{1/2} \quad (21)$$

This is next substituted into (20); the result is the nonlinear Hamilton-Jacobi equation

$$-\frac{\partial V}{\partial \tau} + cT \left(\sqrt{1 + c^{-1} \partial V / \partial T} - \sqrt{T^e / T} \right)^2 = 0 \quad (22)$$

which contains the energy-like (extremum) Hamiltonian of the extremal process

$$H(T, \frac{\partial V}{\partial T}) = cT \left(\sqrt{1 + c^{-1} \partial V / \partial T} - \sqrt{T^e / T} \right)^2 \quad (23)$$

For a positively-defined H , each Hamilton-Jacobi equation for optimal work preserves the general form of autonomous equations known from analytical mechanics and theory of optimal control.

Expressing extremum Hamiltonian (23) in terms of state variable T and Carnot control T' yields an energy-like function satisfying the following relations

$$E(T, u) = f_0 - u \frac{\partial f_0}{\partial u} = cT^e \frac{(T' - T)^2}{T'^2} \quad (24)$$

where E is the Legendre transform of the work lagrangian $l_0 = -f_0$ with respect to the rate $u = dT/d\tau$.

Assuming a numerical value of the Hamiltonian, say h , one can exploit the constancy of H to eliminate $\partial V/\partial T$. Next combining equation $H=h$ with optimal control (21), or with an equivalent result for energy flow control $u=T' - T$

$$u = \left(\frac{T^e T}{1 + c^{-1} \partial V / \partial T} \right)^{1/2} - T \quad (25)$$

yields optimal rate $u=\dot{T}$ in terms of temperature T and the Hamiltonian h

$$\dot{T} = \{\pm\sqrt{h/cT^e} (1 \pm \sqrt{h/cT^e})^{-1}\}T \quad (26)$$

A more general form of this result which applies to systems with internal dissipation (factor Φ) and applies to the pseudo-Newtonian model of radiation is

$$\dot{T} = \left(\pm \sqrt{\frac{h_\sigma}{\Phi c_v(T)}} \left(1 \pm \sqrt{\frac{h_\sigma}{\Phi c_v(T)}} \right)^{-1} \right) T \quad (27)$$

This result is obtained by the application of variational calculus to nonlinear radiation fluids with the temperature dependent heat capacity $c_v(T)=4a_0T^3$. Thus pseudo-Newtonian systems produce power relaxing with the optimal rate

$$\dot{T} = \xi(h_\sigma, T, \Phi)T \quad (28)$$

where ξ , defined on the basis of Eq. (27), is an intensity index, and $h_\sigma=h/T$. Positive ξ refers to heating of the resource fluid in the heat-pump mode, and the negative to cooling of this fluid in the engine mode. Equations (27) and (28) describe the optimal trajectory in terms of state variable T and constant h . The corresponding optimal (Carnot) control is

$$T' = (1 + \xi(h_\sigma, \Phi, T))T \quad (29)$$

The presence of resource temperature T in function ξ proves that, in comparison with the linear systems, the pseudo-Newtonian relaxation curve is not exponential.

Optimal Work Functions for Linear and Pseudo-Newtonian Kinetics

A solution can now be found to the problem of Hamiltonian representation of extremal work. Let us begin with linear systems. Substituting temperature control (29) with a constant ξ into work functional (4) and integrating along an optimal path yields extremal work function

$$V(T^i, T^f, h) = c(T^i - T^f) - cT^e \ln \frac{T^i}{T^f} - cT^e \sqrt{\frac{h}{cT^e}} \ln \frac{T^i}{T^f} \quad (30)$$

This expression is valid for every process mode. Integration of Eq (27), subject to end conditions $T(\tau^i)=T^i$ and $T(\tau^f)=T^f$, allows one to express Eq. (30) in terms of the process duration.

For the radiation $c_v(T)=4a_0T^3$, where a_0 is the radiation constant, an optimal trajectory solving Eqs. (27) and (29) is

$$\begin{aligned} & \pm (4/3)a_0^{1/2}\Phi^{1/2}h_\sigma^{-1/2}\left(T^{3/2} - T^{i3/2}\right) \\ & - \ln(T/T^i) = \tau - \tau^i \end{aligned} \quad (31)$$

The integration limits refer to the initial state (i) and a current state of the radiation fluid, i.e. temperatures T^i and T corresponding with τ^i and τ . Optimal curve (31) refers to the case when the radiation relaxation is subject to a constraint resulting from Eq. (28).

Equation (31) is associated with the entropy production term in Eq. (12). The corresponding extremal work function per unit volume of flowing radiation is

$$\begin{aligned} V \equiv & h_v^i - h_v^f - T^e(s_v^i - s_v^f) - (4/3)a_0^{1/2}h_\sigma^{1/2}\Phi^{1/2}T^e(T^{i3/2} - T^{f3/2}) \\ & + (4/3)a_0T^e(1-\Phi)(T^{i3} - T^{f3}) \end{aligned} \quad (32)$$

Also, the corresponding exergy function, obtained from (32) after applying exergy boundary conditions, has an explicit analytical form. The classical availability of radiation at flow resides in the resulting exergy equation in Jeter's [10] form

$$A_v^{class}(T, T^e, 0) = h_v - h_v^e - T^e(s_v - s_v^e) = h_v(1 - T^e/T) = (4/3)a_0T^4(1 - T^e/T). \quad (33)$$

Work Functions for Chemical Systems

The developed methodology can be extended to chemical and electrochemical engines. Here we shall make only a few basic remarks. In chemical engines, mass transports participate in transformation of chemical affinities into mechanical power [11]. Yet, as opposed to thermal machines, in chemical ones generalized reservoirs are present, capable of

providing both heat and substance. When infinite reservoirs assure constancy of chemical potentials, problems of extremum power (maximum of power produced and minimum of power consumed) are static optimization problems. For finite reservoirs, however, the amount and chemical potential of an active reactant decrease in time, and considered problems are those of dynamic optimization and variational calculus. Because of the diversity and complexity of chemical systems the area of power-producing chemistries is extremely broad. The simplest model of a power-producing chemical engine is that with an isothermal and isomeric reaction, $A_1-A_2=0$ [11]. The power expression and efficiency formula for the chemical system follow from the entropy conservation and energy balance in the power-producing zone of the system (active part). In “endoreversible chemical engines” the total entropy flux is continuous through the active zone. When a formula describing this continuity is combined with energy balance we find in an isothermal case

$$p = (\mu_1 - \mu_2)n \quad (34)$$

where n is an invariant molar flux of reagents. Process efficiency ζ is defined as power yield per molar flux, n , i.e.

$$\zeta = p/n = \mu_1 - \mu_2 \quad (35)$$

This efficiency is identical with the chemical affinity of our reaction in the chemically active part of the system. While ζ is not dimensionless, it correctly describes the system.

For a steady engine the following function defines the chemical efficiency in terms of n and mole fraction x (Fig. 3)

$$\zeta = \zeta_0 + RT \ln \left(\frac{x_1 - ng_1^{-1}}{ng_2^{-1} + x_2} \right) \quad (36)$$

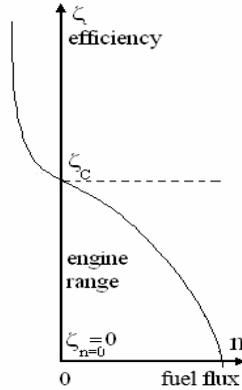


Fig. 3. Efficiency of power production ζ in terms of fuel flux n in a chemical engine.

Equation (36) shows that an effective concentration of the reactant in upper reservoir $x_{1\text{eff}} = x_1 - g_1^{-1}n$ is decreased, whereas an effective concentration of the product in lower reservoir $x_{2\text{eff}} = x_2 + g_2^{-1}n$ is increased due to the finite mass flux. Therefore efficiency ζ decreases nonlinearly with n . When effect of resistances g_k^{-1} is ignorable or flux n is very small, reversible efficiency, ζ_C , is attained. The power function, described by the product $\zeta(n)n$, exhibits a maximum for a finite value of the fuel flux, n .

Application of Eq. (36) to an unsteady system leads to a work function describing the dynamical limit of the system

$$W = - \int_{\tau_i}^{\tau_f} \left\{ \zeta_0 + RT \ln \left(\frac{X/(1+X) + dX/d\tau_1}{x_2 - j dX/d\tau_1} \right) \right\} \frac{dX}{d\tau_1} d\tau_1 \quad (37)$$

($X=x/(1-x)$.) The path optimality condition may be expressed in terms of the constancy of the following Hamiltonian

$$H(X, \dot{X}) = RT\dot{X}^2 \frac{x_2 + jx_1(X)}{x_1(X)x_2} = RT\dot{X}^2 \left(\frac{1+X}{X} + \frac{j}{x_2} \right). \quad (38)$$

For low rates and large concentrations X (mole fractions x_1 close to the unity), optimal relaxation rate is approximately constant. Yet, in an